

Sintering behavior and microwave dielectric properties of a new low-permittivity ceramic system $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$

Huanping Wang^a, Denghao Li^a, Qinghua Yang^a, Ruoshan Lei^a, Hongping Ma^b, Shiqing Xu^{a,*}

^aCollege of Materials Science and Engineering, China Jiliang University, Hangzhou 310018, PR China

^bSchool of Mechanical & Automotive Engineering, Zhejiang University of Science and Technology, Hangzhou 310012, PR China

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Abstract

The diopside ceramics with a formula of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ($x=0.01\text{--}0.3$) were synthesized via a traditional solid-state reaction method, and their solid solubility, sintering behavior and microwave dielectric properties were investigated. The results revealed that the solubility limit of Al_2O_3 in $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$, which is defined as x , was between 0.15 and 0.2, and a second phase of $\text{CaAl}_2\text{SiO}_6$ presented when the x value reached 0.2. Appropriate Al^{3+} substitution for Mg^{2+} and Si^{4+} could promote the sintering process and lower the densification temperature, and a broadened densification temperature range of $1250\text{--}1300\text{ }^\circ\text{C}$ was obtained for the compositions of $x=0.08\text{--}0.15$. With the increase of the x value, the dielectric constant (ϵ_r) increased roughly linearly, and the temperature coefficient of frequency (τ_f) showed a rising trend. The $Q \times f$ values increased from 57,322 GHz to 59,772 GHz as the x value increased from 0.01 to 0.08, and then they were saturated in the range of $x=0.08\text{--}0.2$. Further increase of the x value ($x \geq 0.25$) deteriorated the microwave dielectric properties. Good microwave dielectric properties of $\epsilon_r=7.89$, $Q \times f=59,772\text{ GHz}$ and $\tau_f=-42.12\text{ ppm}/^\circ\text{C}$ were obtained for the ceramics with the composition of $x=0.08$ sintered at $1275\text{ }^\circ\text{C}$.

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1. Introduction

The development of microwave dielectric resonators for application in wireless communication systems such as 3G cellular phones, direct broadcasting satellites, wireless local area networks and global positioning systems has been rapidly progressed in the past decade [1–4]. The available frequencies have therefore been extended from microwave to millimeter-wave ranges because large quantity of information can be transported with a high speed in the later range. A high operating frequency in these microwave applications requires dielectric materials with a low dielectric constant (ϵ_r), a high quality factor ($Q \times f$) and a zero temperature coefficient of resonant frequency (τ_f) [5–7]. Low permittivity can not only minimize the cross-coupling between conductors but also shorten the propagation delay time of electromagnetic signal. Furthermore, high quality factor can increase the frequency

selectivity, while near-zero temperature coefficient of the resonant frequency can ensure the stability of the operating frequency against temperature fluctuations.

Several low-permittivity ceramic systems such as $\text{Li}_3\text{AlB}_2\text{O}_6$, Mg_2TiO_4 , $(\text{Mg}, \text{Zn})\text{Al}_2\text{O}_4$, MWO_4 ($\text{M}=\text{Mg}, \text{Zn}, \text{Ni}, \text{Co}, \text{Li}, \text{Ca}, \text{Te}$), MMoO_4 ($\text{M}=\text{Li}, \text{Zn}, \text{Ca}, \text{Al}, \text{In}$), $\text{M}_3(\text{VO}_4)_2$ ($\text{M}=\text{Mg}, \text{Ba}, \text{Ca}, \text{Bi}$), AMP_2O_7 ($\text{A}=\text{Ca}, \text{Sr}; \text{M}=\text{Zn}, \text{Cu}$) and $\text{Y}_2\text{Ba}(\text{Cu}, \text{Mg})\text{O}_5$ have been investigated for microwave applications [7–22]. Moreover, MSiO_3 ($\text{M}=\text{Mg}, \text{Zn}, \text{Ca}$) ceramics have been proved to be excellent dielectric materials with low dielectric constant and low dielectric loss [5,23–26]. However, the sintering temperature range of pure CaSiO_3 ceramic is relatively narrow. Chakradhar et al. pointed out that it was difficult to obtain dense CaSiO_3 ceramic since its grains grew exceptionally and the bulk CaSiO_3 ceramic became more porous with the increase of the calcination temperature [27]. In our previous work, the sintering behavior and microwave dielectric properties of CaSiO_3 ceramics have been investigated by a traditional solid-state process and a sol–gel method, respectively [28]. The maximum bulk density of CaSiO_3 ceramic sintered at $1340\text{ }^\circ\text{C}$ prepared by the conventional

*Corresponding author. Tel.: +86 571 86835781; fax: +86 571 28889527.

E-mail address: sxucjlu@hotmail.com (S. Xu).

solid-state process is 2.439 g/cm^3 , and the microwave dielectric properties are $\epsilon_r=6.59$ and $Q \times f=13,109 \text{ GHz}$. Whereas for CaSiO_3 ceramic obtained by the sol–gel method, the maximum bulk density is 2.505 g/cm^3 and the microwave dielectric properties are $\epsilon_r=6.69$ and $Q \times f=25,398 \text{ GHz}$. The density value of the above two samples synthesized either by the traditional solid-state method or by the sol–gel method is much smaller than that of the theoretical density of the CaSiO_3 ceramic, which is 2.91 g/cm^3 , indicating that it is difficult to obtain dense CaSiO_3 ceramic.

In order to improve the sintering characteristics and microwave dielectric properties, Sun and co-workers have used Mg^{2+} to substitute Ca^{2+} in the CaSiO_3 host to prepare the CaO-MgO-SiO_2 ceramics for low temperature co-fired ceramic (LTCC) applications [29,30], and $\text{CaMgSi}_2\text{O}_6$ ceramic has been demonstrated as a potential candidate material for high-frequency devices fabrication [30–32]. The neat $\text{CaMgSi}_2\text{O}_6$ ceramic sintered at 1290°C possesses good microwave dielectric properties, e.g. ϵ_r , $Q \times f$ and τ_f are 7.46, 59,638 GHz and $-46 \text{ ppm/}^\circ\text{C}$, respectively [30]. However, the sintering temperature range of neat $\text{CaMgSi}_2\text{O}_6$ ceramic is relatively narrow. In order to improve the sintering property, Zhang and co-workers have used Zn^{2+} to substitute Mg^{2+} in the $\text{CaMgSi}_2\text{O}_6$ host and found that it was limited to broaden the densification temperature range, although Zn^{2+} substitution for Mg^{2+} could lower the sintering temperature [33].

In this work, we studied a new microwave dielectric ceramic system of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ with low permittivity and low loss. In order to broaden the range of the sintering temperature, Al^{3+} was used to substitute Mg^{2+} and Si^{4+} in the $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics, and the solid solubility, sintering behavior, microstructure and microwave dielectric properties of this system were investigated.

2. Experimental procedures

Specimen powders were prepared by a conventional solid-state method using high-purity oxide powders (99.99%) of CaCO_3 , MgO , SiO_2 and Al_2O_3 as raw materials. Stoichiometric proportions of the above powders according to the composition of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ($x=0.01, 0.02, 0.04, 0.06, 0.08, 0.1, 0.15, 0.2, 0.25$, and 0.3) were mixed in ethanol for 24 h with zirconia balls as milling media. The wet mixtures were dried and calcined at $1150\text{--}1250^\circ\text{C}$ for 2 h in air to obtain the $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ phase. The calcined powders were re-mixed. After drying and sieving, the as-prepared powders together with the organic binder (5 wt % polyvinyl alcohol) were uniaxially pressed under a pressure of 135 MPa into cylinders of 15 mm in diameter and 8 mm in thickness. These samples were then sintered in the temperature range of $1225\text{--}1300^\circ\text{C}$ for 2 h in air with a heating rate of 5°C/min .

The bulk densities of the sintered pellets were measured by the Archimedes method using distilled water as medium. The sintered bulks were broken up and ground to powders using an agate mortar. Crystal structures of the powders were performed by the X-ray diffraction (XRD, ARL XTRA) with a $\text{Cu K}\alpha$ radiation

(36 kV, 30 mA, and $2\theta=10\text{--}80^\circ$). The polished surfaces of the ceramics were investigated by scanning electron microscopy (SEM, TM3000) after thermal etching. The dielectric constants ϵ_r and the quality values $Q \times f$ at microwave frequencies were measured by the Hakki–Coleman dielectric resonator method using an Agilent 8719ET (50 MHz to 13.5 GHz) Network Analyzer [34,35]. The temperature coefficient of the resonant frequency τ_f was also measured by the same method in the temperature range from 25°C to 80°C and calculated by the following equation:

$$\tau_f = \frac{f_{80} - f_{25}}{f_{25} \times 55} \times 10^6 \text{ (ppm/}^\circ\text{C)}$$

where f_{80} and f_{25} represent the resonant frequency at 80°C and 25°C , respectively.

3. Results and discussion

In order to examine the chemical properties of the calcined $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ powders and select a suitable calcining temperature, the starting materials were prepared at $1150, 1175, 1200, 1225$ and 1250°C . Fig. 1 shows the X-ray diffraction patterns of $\text{Ca}(\text{Mg}_{0.92}\text{Al}_{0.08})(\text{Si}_{0.96}\text{Al}_{0.04})_2\text{O}_6$ powders calcined at different temperatures for 2 h. The phases existing at each calcining temperature are observed, as illustrated in this figure. It can be seen clearly that the phases of CaSiO_3 (PDF 27-0088), $\text{Ca}_2\text{MgSi}_2\text{O}_7$ (PDF 35-0592), MgO (PDF 45-0946) and SiO_2 (PDF 27-0605) are present at the calcining temperature of 1150°C , accompanied by a small amount of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ (PDF 41-1370). When the calcining temperature is increased from 1150°C to 1200°C , the mixed powders react more and the intensity of major $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ phase is enhanced, whereas those of CaSiO_3 , $\text{Ca}_2\text{MgSi}_2\text{O}_7$, MgO and SiO_2 are weakened. Homogeneous $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ phase with diopside structure can be obtained at about $1225\text{--}1250^\circ\text{C}$. So 1225°C was selected as the calcining temperature.

The crystalline phases in $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics with different x values sintered at 1250°C for 2 h were identified and the XRD diffraction patterns are showed in

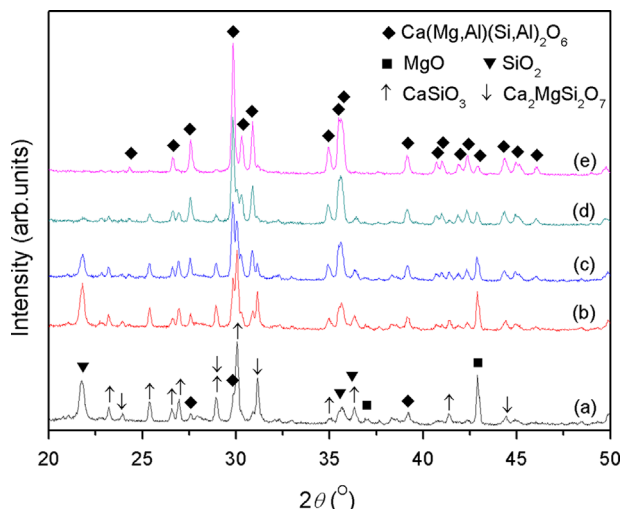


Fig. 1. XRD patterns of $\text{Ca}(\text{Mg}_{0.92}\text{Al}_{0.08})(\text{Si}_{0.96}\text{Al}_{0.04})_2\text{O}_6$ powders calcined at (a) 1150°C , (b) 1175°C , (c) 1200°C , (d) 1225°C and (e) 1250°C .

Fig. 2. As the x value is increased from 0.02 to 0.15, the patterns are similar and match well with $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ (PDF 41-1370), and all of the peaks are indexed without any secondary phases. However, a second phase of $\text{CaAl}_2\text{SiO}_6$ (PDF 31-0249) is observed when the x value reaches 0.2, and the intensity of the second phase peaks increases with the increase of the x value. These results suggest that the solubility limit of Al_2O_3 in $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ is between 0.15 and 0.2. $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ is a chain silicate, crystallizing in monoclinic symmetry with a space group of C2/c , where $a=9.732 \text{ \AA}$, $b=8.867 \text{ \AA}$, $c=5.279 \text{ \AA}$, $\alpha=\gamma=90^\circ$ and $\beta=106.29^\circ$ (PDF 41-1370). Fig. 3 presents the structure of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$. The ionic radii of Mg^{2+} , Si^{4+} and Al^{3+} are $0.72 \text{ \AA}$, $0.40 \text{ \AA}$ and $0.535 \text{ \AA}$, respectively. Based on the equation of $\Delta r=(r_A-r_B)/r_A$, the Δr between Mg^{2+} and Al^{3+} is 25.69%, and that between Si^{4+} and Al^{3+} is 33.75%. These large ionic radii difference results in the limited Al^{3+} substitution for Mg^{2+} and Si^{4+} .

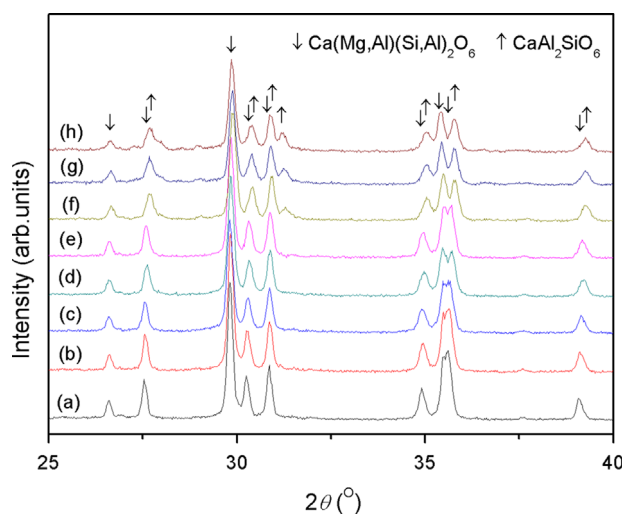


Fig. 2. XRD patterns of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at 1250°C with x value of (a) 0.02, (b) 0.04, (c) 0.08, (d) 0.1, (e) 0.15, (f) 0.2, (g) 0.25 and (h) 0.3.

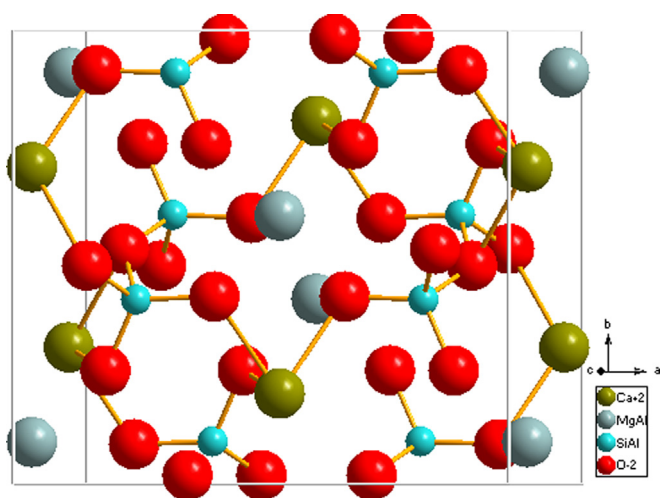


Fig. 3. The structure of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$.

Fig. 4 shows the bulk densities of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at different temperatures. The densification temperatures can be extracted from the plots in this figure. Densification temperatures of 1300°C , 1275°C and 1250°C are obtained for the compositions of $x=0.01$ – 0.02 , $x=0.04$ – 0.1 and $x=0.1$ – 0.15 , respectively. Sintered at 1250°C , the figure shows that the bulk density increases with the increase of the x value from 0.01 to 0.15. These results indicate that the Al^{3+} substitution can promote the sintering process and lower the densification temperature of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramics. For the compositions of $x=0.08$ – 0.15 , a broadened densification temperature range of 1250 – 1300°C is observed. It is also seen from the figure that the bulk density of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at 1250°C decreases with the increase of the x value from 0.15 to 0.3. The $\text{CaAl}_2\text{SiO}_6$ second phase occurs as the x value reaches 0.2 (shown in Fig. 2). Therefore, it is considered that the bulk density of $\text{CaAl}_2\text{SiO}_6$ ceramic is lower than that of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramic. Meanwhile, we have found that the pellets melted when sintered at 1275°C for the compositions of $x=0.25$ – 0.3 and sintered at 1300°C for the compositions of $x=0.2$ – 0.3 , indicating that the melt point of $\text{CaAl}_2\text{SiO}_6$ is about 1250 – 1275°C .

The microstructures of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at 1250°C with different x values are presented in Fig. 5(a)–(f). Fig. 5(a) shows that the average grain size is about $1 \mu\text{m}$ and there are many pores in the bulks, which indicates that $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramic with the x value of 0.02 can be hardly sintered at 1250°C . With the increase of the x value to 0.06, the size of the grains grows and the porosity decreases, as shown in Fig. 5(b). When the x value increases sequentially to 0.08–0.10, the specimens become well-densified as well as rapid grain growth. It indicates that appropriate Al^{3+} substitution ($x=0.08$ – 0.10) can promote the sintering process of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramics, which is consistent with the results of the bulk densities sintered at different temperatures, as shown in Fig. 4.

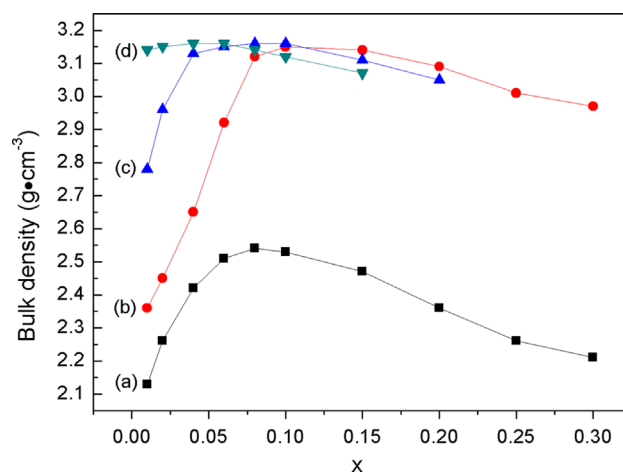


Fig. 4. Bulk densities of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics with different x values sintered at (a) 1225°C , (b) 1250°C , (c) 1275°C and (d) 1300°C .

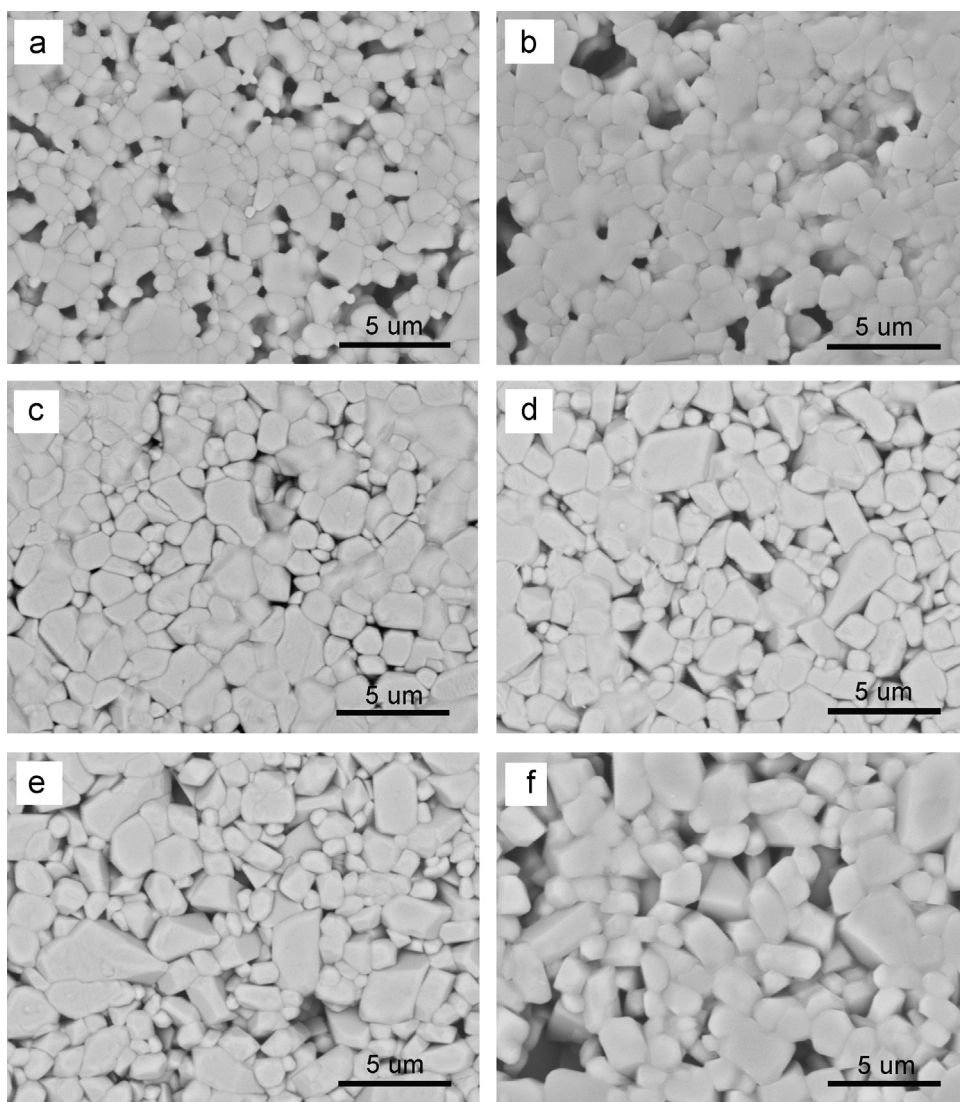


Fig. 5. SEM photographs of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at 1250 °C with x value of (a) 0.02, (b) 0.06, (c) 0.08, (d) 0.1, (e) 0.15 and (f) 0.2.

However, the surface of the ceramics seems to be porous as the x value reaches 0.2. One possible explanation is that the volatilization of the $\text{CaAl}_2\text{SiO}_6$ second phase occurs during thermal etching and results in porosity.

Fig. 6 shows the images of thermally etched surfaces of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at their optimum temperatures with different x values. The evident equiaxed grain morphology is observed for $x=0.01$ – 0.02 , while a certain number of columnar grain morphology is observed for the ceramics with $x=0.08$ – 0.15 . Lattice constants such as $a=9.733$ Å, $b=8.909$ Å, and $c=5.296$ Å for $\text{Ca}(\text{Mg}_{0.7}\text{Al}_{0.3})(\text{Si}_{0.85}\text{Al}_{0.15})_2\text{O}_6$ (ICSD 158207) and $a=9.697$ Å, $b=8.850$ Å, and $c=5.306$ Å for $\text{Ca}(\text{Mg}_{0.5}\text{Al}_{0.5})(\text{Si}_{0.75}\text{Al}_{0.25})_2\text{O}_6$ (ICSD 158208) can be extracted from the XRD patterns, which indicates that the lattice parameter in the c -axis increases with the Al^{3+} substitution, while those in the a - and b -axes decrease. Moreover, the lattice parameter in the c -axis is much smaller than those in the a - and b -axes. So the growth rate of crystal is faster for the c -axis direction than that for the a - and b -axes with Al^{3+} substitution [36,37], which results in columnar

grain morphology for $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics with high x values.

Microwave dielectric properties of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at the optimum temperatures as a function of the x value are illustrated in Table 1 and Fig. 7. The dielectric constant (ϵ_r) increases roughly linearly from 7.79 to 7.95 as the x value increases from 0.01 to 0.15, indicating the Al^{3+} substitution can promote the apparent improvement of the dielectric constant of the $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramics. Further increase of the x value leads to the increase of the ϵ_r eventually to 8.16 for the composition of $x=0.3$. As shown in the XRD patterns (Fig. 2), the solubility limit of Al_2O_3 in $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ is between 0.15 and 0.2, and $\text{CaAl}_2\text{SiO}_6$ second phase occurs as the x value reaches 0.2. Combined with the empirical rule of $\ln \epsilon_r = \sum_i V_i \ln \epsilon_{ri}$, where V_i and ϵ_{ri} are the volume fraction and the permittivity of each phase, respectively [38], we conclude that the dielectric constant of the $\text{CaAl}_2\text{SiO}_6$ second phase is larger than that of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramic.

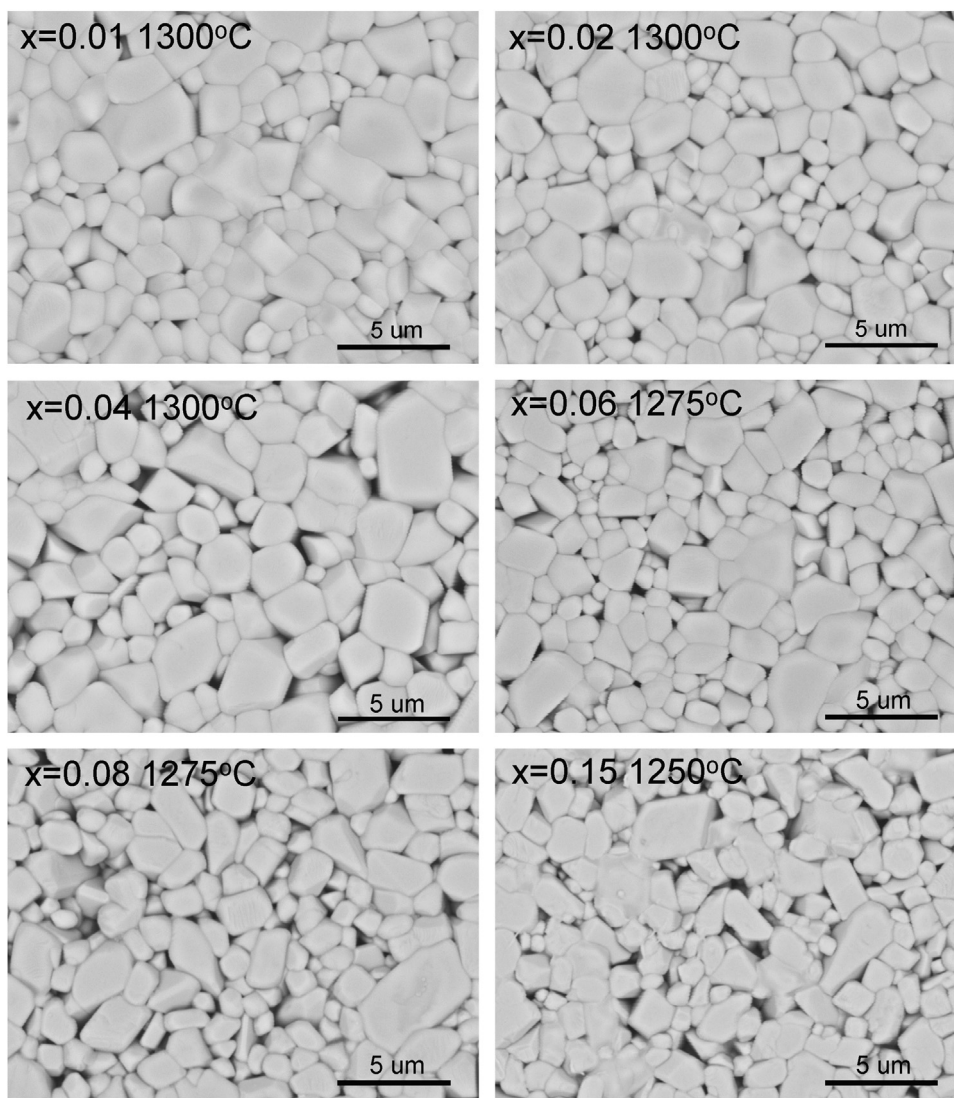


Fig. 6. SEM photographs of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at the optimum temperature with various compositions.

The $Q \times f$ values of the well-sintered $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics increase from 57,322 GHz to 59,772 GHz as the x value increases from 0.01 to 0.08, and then they are saturated in the range of $x=0.08$ –0.2. As the x value reaches 0.3, the $Q \times f$ value decreases dramatically to 43,727 GHz. It was reported that the microwave dielectric loss was mainly caused not only by the lattice vibrational modes, but also by the pores, the grain morphology and the secondary phases. As shown in Fig. 5, high x value ($x=0.2$) results in porosity. In addition, the $\text{CaAl}_2\text{SiO}_6$ second phase occurs as the x value exceeds 0.2. So the $Q \times f$ value decreases with the increase of the x value in the composition range of 0.2–0.3. Combined with the sintering behavior, good microwave dielectric properties of $\epsilon_r=7.89$ and $Q \times f=59,772$ GHz were obtained for the ceramics with the composition of $x=0.08$ sintered at 1275 °C, which possesses a broadened densification temperature range of 1250–1300 °C.

From the temperature coefficient of frequency (τ_f) of well-sintered $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics with the

composition range of 0.01–0.3, it is clear that the τ_f values range from -39.42 to -44.92 ppm/°C and show a rising trend with the increase of the x value. The τ_f is well known to be governed by the composition, the additives and the second phase of the materials. The increase of the τ_f value with the x value increasing may have been caused by the change in the volume of the crystal unit cell. Moreover, it is considered that the τ_f value of $\text{CaAl}_2\text{SiO}_6$ second phase is lower than that of $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ ceramics. In general, because a near-zero τ_f value of dielectric ceramics is necessary for commercial applications, an improvement in τ_f value, closer to 0 ppm/°C, is required in this system.

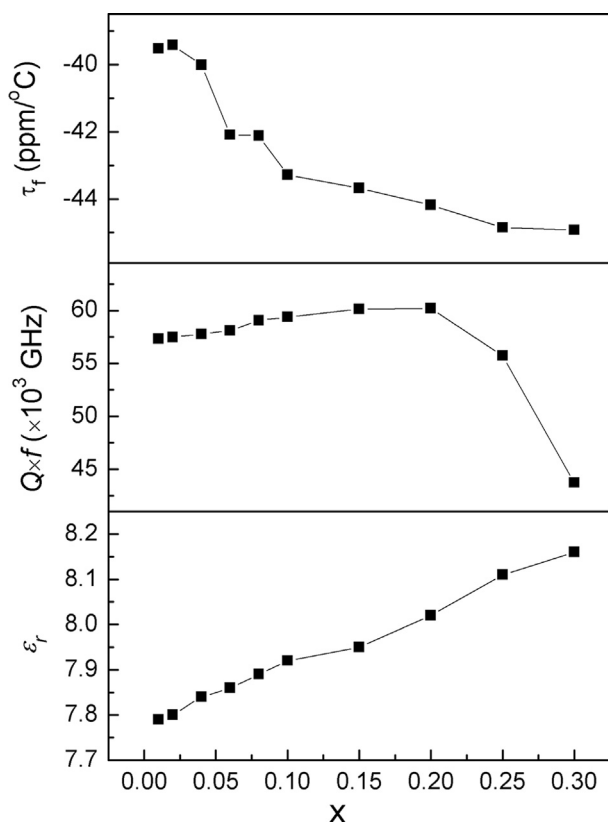
4. Conclusions

The crystalline phases of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics ($x=0.01$ –0.3) showed that the solubility limit of Al_2O_3 in $\text{Ca}(\text{Mg},\text{Al})(\text{Si},\text{Al})_2\text{O}_6$ was between 0.15 and 0.2, and a second phase of $\text{CaAl}_2\text{SiO}_6$ was obtained as the x value reached 0.2. Appropriate Al^{3+} substitution for Mg^{2+} and Si^{4+}

Table 1

Microwave dielectric properties and apparent density of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at the optimum temperature.

$\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$	Diameter (mm)	Height (mm)	ρ (g cm ⁻³)	f_0 (GHz)	ϵ_r	$Q \times f$ (GHz)	τ_f (ppm/°C)
$x=0.01/1300^\circ\text{C}$	12.45	6.10	3.14	11.26	7.79	57,322	-39.52
$x=0.02/1300^\circ\text{C}$	12.44	6.02	3.15	11.32	7.80	57,470	-39.42
$x=0.04/1300^\circ\text{C}$	12.42	6.06	3.16	11.53	7.84	57,770	-40.01
$x=0.06/1275^\circ\text{C}$	12.49	5.98	3.15	11.33	7.86	57,504	-42.09
$x=0.08/1275^\circ\text{C}$	12.49	6.15	3.16	11.40	7.89	59,772	-42.12
$x=0.10/1250^\circ\text{C}$	12.42	6.01	3.15	11.67	7.92	59,387	-43.28
$x=0.15/1250^\circ\text{C}$	12.44	6.04	3.14	11.54	7.95	59,134	-42.68
$x=0.20/1250^\circ\text{C}$	12.47	6.02	3.09	11.31	8.02	60,203	-44.18
$x=0.25/1250^\circ\text{C}$	12.76	5.99	3.01	11.06	8.11	55,734	-43.85
$x=0.30/1250^\circ\text{C}$	12.82	6.12	2.97	10.89	8.16	43,727	-44.92

Fig. 7. Microwave dielectric properties of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics sintered at the optimum temperature as a function of the composition x .

could promote the sintering process and lower the densification temperature of $\text{Ca}(\text{Mg}_{1-x}\text{Al}_x)(\text{Si}_{1-x/2}\text{Al}_{x/2})_2\text{O}_6$ ceramics. The densification temperatures were 1300°C , 1275°C and 1250°C for the compositions of $x=0.01$ – 0.02 , $x=0.04$ – 0.08 and $x=0.1$ – 0.3 , respectively. Meanwhile, a broadened densification temperature range of 1250 – 1300°C was obtained for the compositions of $x=0.08$ – 0.15 . With the x value increase from 0.01 to 0.3 , the dielectric constant (ϵ_r) increased roughly linearly from 7.79 to 8.16 , and the temperature coefficient of frequency (τ_f) showed a rising trend ranging from -39.42 to -44.92 ppm/°C. The $Q \times f$ values increased from $57,322$ GHz to $59,772$ GHz as the x value increased from 0.01 to 0.08 , and then they were saturated in the range of $x=0.08$ – 0.2 . However,

further increase of the x value ($x \geq 0.25$) deteriorated the microwave dielectric properties. Combined with the sintering behavior, good microwave dielectric properties of $\epsilon_r=7.89$, $Q \times f=59,772$ GHz and $\tau_f=-42.12$ ppm/°C were obtained for the ceramics with the composition of $x=0.08$ sintered at 1275°C .

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